

SAMPLE HINTS AND SOLUTIONS

INSTITUTE NAME & LOGO

MHT-CET – EXAM YEAR

Time : 90 Min

Maths : Full Portion Paper

Marks : 100

Hints and Solutions

201) Ans: **C) 2**

Sol: The curves $y = x$ and $y = x + \sin x$ intersect at $(0, 0)$ and (π, π) .

\therefore Area bounded by the two curves

$$= \int_0^\pi (x + \sin x) dx - \int_0^\pi x dx = \int_0^\pi \sin x dx \\ = [-\cos x]_0^\pi = -\cos \pi + \cos 0 = -(-1) + (1) = 2$$

202) Ans: **B) $-\frac{1}{5}\cos^5 x + \frac{2}{7}\cos^7 x - \frac{1}{9}\cos^9 x + c$**

Sol: Put $\cos x = t \Rightarrow -\sin x dx = dt$, in the given integral

$$\int (1 - \cos^2 x)^2 \cdot \cos^4 x \sin x dx = - \int (1 - t^2)^2 \cdot t^4 dt \\ = -\frac{t^5}{5} + \frac{2}{7}t^7 - \frac{1}{9}t^9 + c \\ = -\frac{\cos^5 x}{5} + \frac{2}{7}\cos^7 x - \frac{1}{9}\cos^9 x + c$$

203) Ans: **B) $2\bar{a} + 5\bar{b} + 3\bar{c}$**

Sol: Let us suppose that $\bar{R} = x\bar{a} + y\bar{b} + z\bar{c}$
 $\Rightarrow \bar{R} = x(2\bar{p} + 3\bar{q} - \bar{r}) + y(\bar{p} - 2\bar{q} + 2\bar{r}) + z(-2\bar{p} + \bar{q} - 2\bar{r})$
 $\Rightarrow 3\bar{p} - \bar{q} + 2\bar{r} = (2x + y - 2z)\bar{p} + (3x - 2y + z)\bar{q} + (-x + 2y - 2z)\bar{r}$

Comparing... we get,

$$2x + y - 2z = 3, \quad 3x - 2y + z = -1, \\ -x + 2y - 2z = 2$$

Solving above equations, we get

$$X = 2, y = 5, z = 3$$

$$\therefore \bar{R} = 2\bar{a} + 5\bar{b} + 3\bar{c}$$

204) Ans: **C) $\frac{5}{\sqrt{2}}$**

Sol: Equations of lines are

$$\bar{r} = (-\hat{i} + \hat{j} - \hat{k}) + \lambda(\hat{i} + \hat{j} - \hat{k}) \text{ and}$$

$$\bar{r} = (\hat{i} - \hat{j} + 2\hat{k}) + \mu(-\hat{i} + 2\hat{j} + \hat{k})$$

Shortest distance

$$= \frac{\begin{vmatrix} 1+1 & -1-1 & 2+1 \\ 1 & 1 & -1 \\ -1 & 2 & 1 \end{vmatrix}}{\sqrt{(1+2)^2 + (1-1)^2 + (2+1)^2}} \\ = \frac{2(3) + 2(0) + 3(3)}{3\sqrt{2}} = \frac{5}{\sqrt{2}}$$

205) Ans: **A) $a - b - c$**

$$\text{Sol: } \begin{vmatrix} a & 1 & 1 \\ 1 & -b & 1 \\ 1 & 1 & -c \end{vmatrix} = 0$$

$$\therefore a(bc - 1) - 1(-c - 1) + 1(1 + b) = 0$$

$$abc - a + c + 1 + 1 + b = 0$$

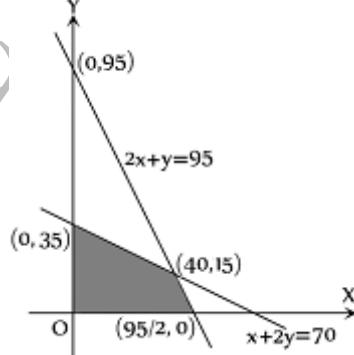
$$\Rightarrow abc + 2 = a - b - c$$

206) Ans: **C) $n\pi \pm \frac{\pi}{4}$**

$$\text{Sol: } 2\tan^2 \theta = \sec^2 \theta \Rightarrow 2\tan^2 \theta = \tan^2 \theta + 1$$

$$\Rightarrow \tan^2 \theta = 1 = \tan^2 \left(\frac{\pi}{4} \right) \therefore \theta = n\pi \pm \frac{\pi}{4}$$

207) Ans: **A) (40, 15)**



Sol:

The shaded region represents feasible region.

\therefore Max $z = x + y$.

It is obvious that, it is maximum at (40, 15).

208) Ans: **A) 8, 8**

Sol:

$$x + y = 16 \Rightarrow y = 16 - x \Rightarrow x^2 + y^2 = x^2 + (16 - x)^2$$

$$\text{Let, } z = x^2 + (16 - x)^2 \Rightarrow z' = 4x - 32$$

To be minimum of z , $z'' > 0$,

$$\therefore 4x - 32 = 0 \Rightarrow x = 8 \quad y = 8$$

209) Ans: **B) $\bar{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \lambda(\hat{i} - 2\hat{j} + 3\hat{k})$**

$$\frac{x-1}{1} = \frac{y-2}{-2} = \frac{z-3}{3}$$

Sol: Since, the required line passes through the point (1, 2, 3) and parallel to $\hat{i} - 2\hat{j} + 3\hat{k}$, the vector equation of the line is $\bar{r} = (\hat{i} + 2\hat{j} + 3\hat{k}) + \lambda(\hat{i} - 2\hat{j} + 3\hat{k})$;

The Cartesian equation of the line is

$$\frac{x-1}{1} = \frac{y-2}{-2} = \frac{z-3}{3}$$

210) Ans: B) $(1, \pm 2)$

$$\text{Sol: } \frac{d}{dx}(x^2 + y^2 - 2x - 3) = 0 \Rightarrow 2x + 2y \frac{dy}{dx} - 2 = 0$$

$$\therefore \frac{dy}{dx} = \frac{1-x}{y}$$

As the tangent is parallel to X-axis,

$$\therefore \frac{1-x}{y} = 0 \text{ i.e. } x = 1 \therefore y = \pm 2$$

Thus the point is $(1, \pm 2)$.

211) Ans: B) $\frac{16}{27}$

$$\text{Sol: Probability of failure} = \frac{1}{3}$$

$$\text{and Probability for getting success} = \frac{2}{3}$$

\therefore Required probability

$$= {}^4C_4 \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^0 + {}^4C_3 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)$$

$$= \left(\frac{2}{3}\right)^4 + 4 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right) = \frac{16}{27}$$

	X:	0	1	2	3	4
P(X):	0.1	0.3	0.6	0.75	1	

$$\text{Sol: } F(x_1) = p_1 = 0.1$$

$$F(x_2) = p_1+p_2 = 0.1+0.2 = 0.3$$

$$F(x_3) = p_1+p_2+p_3 = 0.1+0.2+0.3 = 0.6$$

$$F(x_4) = p_1+p_2+p_3+p_4 = 0.1+0.2+0.3+0.15 = 0.75$$

$$F(x_5) = p_1+p_2+p_3+p_4+p_5 = 0.1+0.2+0.3+0.15+0.25 = 1$$

213) Ans: D) $\frac{1}{\sqrt{3}} \tan^{-1} \left(\frac{2x^2 + 1}{\sqrt{3}} \right) + c$

$$\text{Sol: Let } I = \int \frac{x}{x^4 + x^2 + 1} dx$$

$$\text{Put } x^2 = t \Rightarrow 2x dx = dt \Rightarrow x dx = \frac{1}{2} dt$$

$$\therefore I = \frac{1}{2} \int \frac{dt}{t^2 + t + 1} = \frac{1}{2} \int \frac{dt}{t^2 + t + \frac{1}{4} + \frac{3}{4}}$$

$$= \frac{1}{2} \int \frac{dt}{(t + 1/2)^2 + \left(\frac{\sqrt{3}}{2}\right)^2}$$

$$= \frac{1}{2} \cdot \frac{1}{(\sqrt{3}/2)} \tan^{-1} \left(\frac{t + 1/2}{\sqrt{3}/2} \right) + c$$

$$= \frac{1}{\sqrt{3}} \tan^{-1} \left(\frac{2t+1}{\sqrt{3}} \right) + c = \frac{1}{\sqrt{3}} \tan^{-1} \left(\frac{2x^2 + 1}{\sqrt{3}} \right) + c$$

214) Ans: A) $1 - (2.9)(0.9)^{19}$

Sol: Let p denotes the probability that light has not useful life and q denotes useful life, then

$$q = 0.9 \quad p = 1 - q = 1 - 0.9 = 0.1$$

Here n = 20

The probability that at least 2 lights will not have a useful life is

$$P(X \geq 2) = 1 - (X < 2)$$

$$P(X \geq 2) = 1 - (P(X = 0) + P(X = 1))$$

$$P(X \geq 2) = 1 - {}^{20}C_0(0.1)^0 (0.9)^{20} - {}^{20}C_1(0.1)^1 (0.9)^{19}$$

$$P(X \geq 2) = 1 - (1)(1)(0.9)^{20} - (20)(0.1)(0.9)^{19}$$

$$P(X \geq 2) = 1 - (0.9 + 2)(0.9)^{19}$$

$$P(X \geq 2) = 1 - (2.9)(0.9)^{19}$$

215) Ans: B) $\frac{-4 \pm 3\sqrt{2}}{3}$

$$\text{Sol: } \cos \theta = \frac{a_1 a_2 + b_1 b_2 + c_1 c_2}{\sqrt{a_1^2 + b_1^2 + c_1^2} \sqrt{a_2^2 + b_2^2 + c_2^2}}$$

$$\Rightarrow \cos \left(\frac{\pi}{4} \right) = \frac{(1)(1) + (2)(3k) + (1)(1)}{\sqrt{1+4+1} \sqrt{1+9k^2+1}}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{1+6k+1}{\sqrt{6} \sqrt{9k^2+2}} \Rightarrow \frac{1}{2} = \frac{(6k+2)^2}{6(9k^2+2)}$$

$$\Rightarrow 6(9k^2+2) = 8(3k+1)^2 \Rightarrow 27k^2 + 6 = 36k^2 + 24k + 4$$

$$\Rightarrow 9k^2 + 24k - 2 = 0$$

$$\Rightarrow k = \frac{-24 \pm \sqrt{576+72}}{18} = \frac{-24 \pm \sqrt{648}}{18}$$

$$\Rightarrow k = \frac{-24 \pm 18\sqrt{2}}{18} = \frac{-4 \pm 3\sqrt{2}}{3}$$

216) Ans: C) $3 : 2$

$$\text{Sol: } 2\bar{a} + 3\bar{b} - 5\bar{c} = \bar{0}$$

$$\therefore 5\bar{c} = 2\bar{a} + 3\bar{b} \quad \therefore \bar{c} = \frac{3\bar{b} + 2\bar{a}}{3+2}$$

217) Ans: C) $\frac{2xy}{2y - x^2}$

$$\text{Sol: } y = x^2 + \frac{1}{y} \Rightarrow y^2 = x^2 y + 1$$

$$\Rightarrow 2y \frac{dy}{dx} = y \cdot 2x + x^2 \frac{dy}{dx} \quad \therefore \frac{dy}{dx} = \frac{2xy}{2y - x^2}$$

218) Ans: D) $y'' = -\omega^2 y$

$$\text{Sol: } y = A \cos \omega t + B \sin \omega t$$

$$\therefore y' = -A\omega \sin \omega t + B\omega \cos \omega t$$

$$\therefore y'' = -A\omega^2 \cos \omega t - B\omega^2 \sin \omega t$$

$$\Rightarrow y'' = -\omega^2(A \cos \omega t + B \sin \omega t) \quad \therefore y = -\omega^2 y$$

219) Ans: B) $-\frac{2}{5}$

Sol: From given, $|A| = -20$

$$\therefore a_{23} = \frac{\text{Co-factor of } 6}{-20} = \frac{-8}{20} = \frac{-2}{5}$$

220) Ans: C) $\tan x + c$

Sol: Since, $a^{\log_a m} = m$

$$\therefore \int 9^{\log_3(\sec x)} dx = \int \sec^2 x dx \quad \dots \quad \begin{aligned} &\because 3^{2\log_3(\sec x)} \\ &= 3^{\log_3(\sec x)^2} \\ &= (\sec x)^2 \end{aligned}$$

221) Ans: D) 4/3

Sol: Suppose, $I = \int_0^\pi |\sin^3 \theta| d\theta$

As $\sin\theta$ is positive in interval $(0, \pi)$

$$\begin{aligned} \therefore I &= \int_0^\pi \sin^3 \theta d\theta = \int_0^\pi \sin \theta (1 - \cos^2 \theta) d\theta \\ &= \int_0^\pi \sin \theta d\theta + \int_0^\pi (-\sin \theta) \cos^2 \theta d\theta \\ &= [-\cos \theta]_0^\pi + \left[\frac{\cos^3 \theta}{3} \right]_0^\pi = \frac{4}{3} \end{aligned}$$

222) Ans: A) $\tan^{-1}(-2)$

Sol: Here, $m_1 + m_2 = \frac{2\tan A}{-1} = 4$

$\Rightarrow \tan A = -2 \quad \therefore \angle A = \tan^{-1}(-2)$

223) Ans: D) 2

Sol: $\cot \frac{B}{2} \cdot \cot \frac{C}{2} = \sqrt{\frac{s(s-b)}{(s-a)(s-c)} \cdot \frac{s(s-c)}{(s-a)(s-b)}}$

$$\begin{aligned} &= \frac{s}{s-a}, \text{ {As } } 3a = b+c \text{ or } a+b+c = 2s = 4a \\ &= 2a/a = 2 \end{aligned}$$

224) Ans: A) 2

Sol: Since $f(x)$ is continuous at $x = 0$, therefore

$$f(0) = \lim_{x \rightarrow 0} f(x) = \lim_{x \rightarrow 0} \frac{(27-2x)^{1/3} - 3}{9 - 3(243+5x)^{1/5}}, \left(\text{form } \frac{0}{0} \right)$$

By L - Hospital rule

$$f(0) = \lim_{x \rightarrow 0} \frac{\frac{1}{3}(27-2x)^{-2/3}(-2)}{-\frac{3}{5}(243+5x)^{-4/5}(5)} = 2$$

225) Ans: B) $\sin x$

Sol: Considering the $f(x) = \sin x$

$\therefore f(0) = 0$ and $f'(x) = \cos x \Rightarrow f'(0) = 1$

Also, $f'(x) = -\sin x = -f(x)$

226) Ans: A) 0

Sol: Suppose, $f(\theta) = \log(\sec \theta - \tan \theta)$

$\Rightarrow f(-\theta) = \log(\sec \theta + \tan \theta)$

$$= \log\left(\frac{1}{\sec \theta - \tan \theta}\right) = \log(\sec \theta - \tan \theta) = -f(\theta)$$

$\therefore f(\theta)$ is an odd function

$$\Rightarrow \int_{-\pi/4}^{\pi/4} \log(\sec \theta - \tan \theta) d\theta = 0$$

227) Ans: D) $\frac{4}{3}$

Sol: $y^2 = x$ and $2y = x \Rightarrow y^2 = 2y \quad \therefore y = 0, 2$

\therefore Required area = $\int_0^2 (y^2 - 2y) dy$

$$= \left(\frac{y^3}{3} - y^2 \right)_0^2 = \frac{4}{3} \text{ sq. unit.}$$

228) Ans: C) 2

Sol: $3 \frac{d^2y}{dx^2} = \left\{ 1 + \left(\frac{dy}{dx} \right)^2 \right\}^{3/2}$

By squaring, we get $9 \left(\frac{d^2y}{dx^2} \right)^2 = \left\{ 1 + \left(\frac{dy}{dx} \right)^2 \right\}^3$

So, the highest derivative is with power 2.

\therefore Degree = 2

229) Ans: D) obtuse angled

Sol: Here, $\cos \theta = \frac{36 + 100 - (-14)^2}{2 \cdot 6 \cdot 10} \quad \therefore \theta = 120^\circ$

230) Ans: D)

$\frac{3}{2}(x \cot^3 x)^{1/2} [\cot^3 x - 3x \cot^2 x \operatorname{cosec}^2 x]$

Sol: $y = (x \cot^3 x)^{3/2}$
 $\Rightarrow \frac{dy}{dx} = \frac{3}{2}(x \cot^3 x)^{1/2} [\cot^3 x + 3x \cot^2 x (-\operatorname{cosec}^2 x)]$
 $= \frac{3}{2}(x \cot^3 x)^{1/2} [\cot^3 x - 3x \cot^2 x \operatorname{cosec}^2 x]$

231) Ans: B) $\frac{\pi}{4}$

Sol: Let $I = \int_0^1 \frac{dx}{x + \sqrt{1-x^2}}$,

Putting $x = \sin \theta, dx = \cos \theta d\theta$,

$$I = \int_0^{\pi/2} \frac{\cos \theta d\theta}{\sin \theta + \cos \theta} = \frac{\pi}{4}$$

232) Ans: B) $\frac{\pi}{3}$

Sol: The principal value of $\sin^{-1} \left[\sin \left(\pi - \frac{2\pi}{3} \right) \right]$

$$= \sin^{-1} \left[\sin \left(\frac{\pi}{3} \right) \right] = \frac{\pi}{3}$$

233) Ans: C) 4

Sol: $A = \begin{bmatrix} x & -2 \\ 3 & 7 \end{bmatrix} \quad \text{adj } A = \begin{bmatrix} 7 & 2 \\ -3 & x \end{bmatrix} \quad |A| = 7x + 6$

$$A^{-1} = \frac{\text{adj } A}{|A|} = \begin{bmatrix} \frac{7}{(7x+6)} & \frac{2}{(7x+6)} \\ \frac{-3}{7x+6} & \frac{x}{7x+6} \end{bmatrix} \quad \dots \text{(i)}$$

$$A^{-1} = \begin{bmatrix} \frac{7}{34} & \frac{1}{17} \\ \frac{-3}{34} & \frac{2}{17} \end{bmatrix} \quad \dots \text{(ii) [Given]}$$

From (i) and (ii), we get

$$\begin{bmatrix} \frac{7}{7x+6} & \frac{2}{7x+6} \\ \frac{-3}{7x+6} & \frac{x}{7x+6} \end{bmatrix} = \begin{bmatrix} \frac{7}{34} & \frac{1}{17} \\ \frac{-3}{34} & \frac{2}{17} \end{bmatrix}$$

$$\Rightarrow \frac{7}{7x+6} = \frac{7}{34} \Rightarrow 7x+6 = 34 \Rightarrow x = 4$$

234) Ans: **D)** $\frac{7}{3}$

Sol: $P(1) = k; P(2) = 2k; P(3) = 3k$

$$\sum_{x_i=S} P(X=x) = 1 \Rightarrow k + 2k + 3k = 1 \quad \therefore k = \frac{1}{6}$$

$$E(X) = \sum xP(x)$$

$$\Rightarrow E(X) = (1)(k) + (2)(2k) + (3)(3k) = k + 4k + 9k$$

$$\Rightarrow E(X) = 14k = \frac{14}{6} = \frac{7}{3}$$

235) Ans: **D)** continuous at $x = 2$ and discontinuous at $x = 3$

$$\text{Sol: } \lim_{x \rightarrow 2^-} (4 - 3x) = 4 - 6 = -2$$

$$\lim_{x \rightarrow 2^+} (2x - 6) = 4 - 6 = -2$$

$$\lim_{x \rightarrow 3^-} (2x - 6) = 6 - 6 = 0$$

$$\lim_{x \rightarrow 3^+} (x + 5) = 3 + 5 = 8$$

$$\therefore \lim_{x \rightarrow 3^-} f(x) \neq \lim_{x \rightarrow 3^+} f(x)$$

236) Ans: **C)** $(-\infty, \infty)$

$$\text{Sol: } f(x) = \frac{x}{1+|x|}$$

$$f'(x) = \frac{1+|x|-x\frac{|x|}{x}}{(1+|x|)^2} = \frac{1}{(1+|x|)^2}$$

Hence, it is differentiable at $(-\infty, \infty)$

237) Ans: **C)** coplanar

$$\text{Sol: } \frac{x}{1} = \frac{y-2}{2} = \frac{z+3}{3} \text{ and } \frac{x-2}{1} = \frac{y-6}{3} = \frac{z-3}{4}$$

The direction ratios of the first line are $(1, 2, 3)$

The direction ratios of the second line are $(2, 3, 4)$

$$\text{i.e. } \frac{2}{1} \neq \frac{3}{2} \neq \frac{4}{3}$$

\therefore The lines are not parallel.

Sum of the products of the direction ratios are not same. i.e. $2 \times 1 + 2 \times 3 + 3 \times 4 \neq 0$

\therefore The lines are not perpendicular.

$$\text{Let } L_1 : \frac{x}{1} = \frac{2y-2}{2} = \frac{z+3}{3}$$

$$L_2 : \frac{x-2}{2} = \frac{y-6}{3} = \frac{z-3}{4}$$

$$\text{Consider } \begin{vmatrix} 0+2 & -2+6 & 3+3 \\ 1 & 2 & 3 \\ 2 & 3 & 4 \end{vmatrix} = \begin{vmatrix} 2 & 4 & 6 \\ 1 & 2 & 3 \\ 2 & 3 & 4 \end{vmatrix}$$

$$= 2 \begin{vmatrix} 1 & 2 & 3 \\ 1 & 2 & 3 \\ 2 & 3 & 4 \end{vmatrix} = 0$$

Since two rows are same, \therefore Determinant is 0.

\therefore The two lines are coplanar

238) Ans: **A)** $\sim(p \wedge \sim q)$

Sol: p: Intelligent persons are polite.

q: Intelligent persons are helpful.

239) Ans: **A)** $c(a+b) = 0$

$$\text{Sol: } ab(0) + 2\left(\frac{c}{2}\right)\left(\frac{c}{2}\right)(0) - a\left(\frac{c}{2}\right)^2 - b\left(\frac{c}{2}\right)^2 - 0(0)^2 = 0$$

$$\therefore ac^2 + bc^2 = 0 \Rightarrow c^2(a+b) = 0 \therefore c(a+b) = 0$$

240) Ans: **D)** $2 \cos 2x$

$$\text{Sol: } \frac{d}{dx} \{\sin(2\cos^{-1}(\sin x))\}$$

$$= \frac{d}{dx} \left\{ \sin \left(2\cos^{-1} \left(\cos \left(\frac{\pi}{2} - x \right) \right) \right) \right\}$$

$$= \frac{d}{dx} \left\{ \sin \left(2 \left(\frac{\pi}{2} - x \right) \right) \right\} = \frac{d}{dx} \{\sin(\pi - 2x)\}$$

$$= -2, \cos(\pi - 2x) \} = 2 \cos 2x$$

241) Ans: **B)** $\log\left(\frac{x}{1-x}\right) - \frac{1}{x} + c$

$$\text{Sol: } \int \frac{dx}{x^2 - x^3} = \int \frac{(1-x)dx}{x^2(1-x)} + \int \frac{x dx}{x^2(1-x)}$$

$$= -\frac{1}{x} + \int \frac{dx}{x(1-x)} = -\frac{1}{x} + \int \frac{dx}{x} + \int \frac{dx}{1-x}$$

$$= -\frac{1}{x} + \log x - \log(1-x) + c = \log\left(\frac{x}{1-x}\right) - \frac{1}{x} + c$$

242) Ans: **B)** $x^2y = c$

$$\text{Sol: } x^2 dy = -2xy dx \Rightarrow \frac{1}{y} dy = -\frac{2x}{x^2} dx$$

By integrating, we get,

$$\log y = -2 \log x + \log c$$

$$\Rightarrow \log y = \log x^{-2} + \log c$$

$$\Rightarrow \log y x^2 = \log c \Rightarrow yx^2 = c$$

243) Ans: **C)** singular matrix

$$\text{Sol: } A (\text{adj } A) = |A|I$$

$\therefore |A| (\text{adj } A) = |A|^n$ (If A is of order $n \times n$)

$$\therefore |A| | \text{adj } A | = |A|^n$$

$$|\text{adj } A| = |A|^{n-1}$$

Since, A is singular

$$\therefore |A| = 0$$

$$\therefore |\text{adj } A| = 0$$

Hence, adj A is a singular matrix.

244) Ans: **C)** $\frac{-3}{2}$

Sol: Let

$$A \equiv (4, 1, 2), B \equiv (5, k, 0), C \equiv (2, 1, 1), D \equiv (3, 3, -1)$$

The direction ratio of line AB are

$$a_1 = 5 - 4 = 1, b_1 = k - 1, c_1 = 0 - 2 = -2$$

The direction ratio of line CD are

$$a_2 = 3 - 2 = 1, b_2 = 3 - 1 = 2, c_2 = -1 - 1 = -2$$

Line AB \perp Line CD, then

$$a_1 a_2 + b_1 b_2 + c_1 c_2 = 0$$

$$\Rightarrow 1 + 2k - 2 + 4 = 0 \Rightarrow 2k = -3 \Rightarrow k = \frac{-3}{2}$$

245) Ans: **C)** $b < -1$

Sol: Let, $f(x) = \sin x - b x + c$

$\therefore f'(x) = \cos x - b > 0$ i.e. $\cos x > b$ or $b < -1$.

246) Ans: **A)** $ax + by + 1 = 0, x + y = 0$

Sol: $ax^2 + (a+b)xy + by^2 + x + y = 0$

$\Rightarrow ax^2 + bxy + x + axy + by^2 + y = 0$

$\Rightarrow x(ax + by + 1) + y(ax + by + 1) = 0$

$\Rightarrow (x + y)(ax + by + 1) = 0$

247) Ans: **D)** $\frac{x-1}{1} = \frac{y-2}{2} = \frac{z-3}{-5}$

Sol: The line passing through point (1, 2, 3) is

$$\frac{x-1}{a} = \frac{y-2}{b} = \frac{z-3}{c}$$

Also, it is perpendicular to the plane

$$x + 2y - 5z + 9 = 0$$

\therefore The equation of line becomes

$$\frac{x-1}{1} = \frac{y-2}{2} = \frac{z-3}{-5}$$

248) Ans: **D)** $\frac{1}{2}(x\sec^2 x - \tan x) + c$

Sol: Let $I = \int x \sin x \sec^3 x \, dx$

$$= \int x \sin x \cdot \frac{1}{\cos^3 x} \, dx = \int x \tan x \cdot \sec^2 x \, dx$$

Put $\tan x = t \Rightarrow \sec^2 x \, dx = dt$ and $x = \tan^{-1} t$

$$\therefore I = \int \tan^{-1} t \cdot t \, dt = \tan^{-1} t \cdot \frac{t^2}{2} - \int \frac{1}{1+t^2} \cdot \frac{t^2}{2} \, dt$$

$$= \frac{t^2 \tan^{-1} t}{2} - \frac{1}{2} \int \left(\frac{t^2+1-1}{1+t^2} \right) dt$$

$$= \frac{t^2 \tan^{-1} t}{2} - \frac{1}{2} \int \left(1 - \frac{1}{1+t^2} \right) dt$$

$$= \frac{t^2 \tan^{-1} t}{2} - \frac{1}{2} t + \frac{1}{2} \tan^{-1} t + c$$

$$= \frac{x \tan^2 x}{2} - \frac{1}{2} \tan x + \frac{1}{2} x + c$$

$$= \frac{x(\sec^2 x - 1)}{2} - \frac{1}{2} \tan x + \frac{1}{2} x + c$$

$$= \frac{1}{2}(x\sec^2 x - \tan x) + c$$

249) Ans: **C)** tautology

Sol:

p	q	$p \wedge q$	$p \vee q$	$(p \wedge q) \rightarrow (p \vee q)$
T	T	T	T	T
T	F	F	T	T
F	T	F	T	T
F	F	F	F	T

250) Ans: **D)** a quadrilateral

Sol: The common region is quadrilateral.